

7.

$$\text{z.z.: } Y = \alpha + \beta X$$

$$\Rightarrow \bar{Y} = \alpha + \beta \bar{X}$$

$$\bar{Y} = \frac{1}{n} \sum_{i=1}^n y_i =$$

$$\bar{Y} = \frac{1}{n} \sum_{i=1}^n (\alpha + \beta x_i) =$$

$$= \bar{Y} = \frac{1}{n} \sum_{i=1}^n \alpha + \beta \frac{1}{n} \sum_{i=1}^n x_i$$

$$= \bar{Y} = \frac{1}{n} n \cdot \alpha + \beta \bar{X}$$

$$\text{z.z. } Y = \alpha + \beta X \Rightarrow s_y^2 = \beta^2 s_x^2$$

$$s_y^2 = \frac{1}{n} \sum_{i=1}^n (y_i - \bar{Y})^2 =$$

$$= \frac{1}{n} \sum_{i=1}^n (\alpha + \beta x_i - (\alpha + \beta \bar{X}))^2 =$$

$$= s_y^2 = \frac{1}{n} \sum_{i=1}^n (\alpha + \beta x_i - \alpha - \beta \bar{X})^2 =$$

$$= s_y^2 = \frac{1}{n} \sum_{i=1}^n (\beta x_i - \beta \bar{X})^2 = \beta^2 \frac{1}{n} \sum_{i=1}^n (x_i - \bar{X})^2$$

$$= \beta^2 s_x^2$$